

Origin of the Difference of the Jovian and Saturnian Satellite Systems

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Sasaki, Stewart & Ida (2010) *ApJ* **714**, 1052

Jovian System v.s. Saturnian System

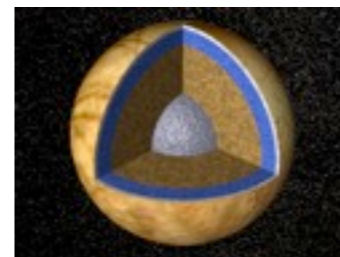


rocky



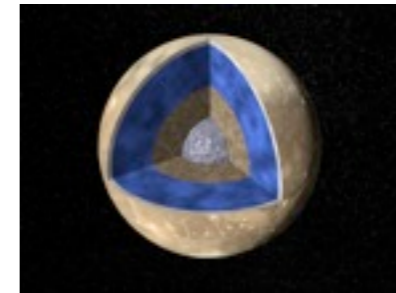
Io

rocky



Europa

icy



Ganymede

icy, undiff.

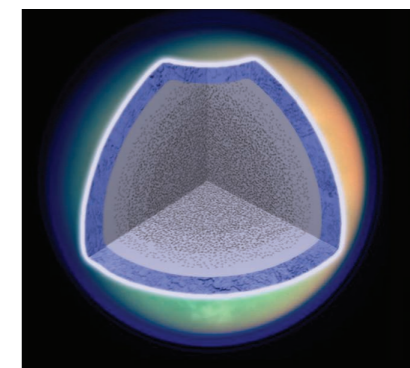


Callisto

mutual mean motion resonances (MMR)



icy, undiff.



only one big body

Titan

Satellite Properties

	a/R_p	$M/M_p [10^{-5}]$	$\rho [g/cm^3]$	C/MR^2
Io	5.9	4.70	3.53	0.378
Europa	9.4	2.53	2.99	0.346
Ganymede	15.0	7.80	1.94	0.312
Callisto	26.4	5.69	1.83	0.355
Titan	20.3	23.7	1.88	0.34

Callisto and Titan's undifferentiated interiors

→ accretion timescale $> 5 \times 10^5$ years [Barr & Canup, 2008]

Questions; Motivation of this study

Satellites' size, number, and location

Jovian: 4 similar mass satellites in MMR

Saturnian: only 1 large satellite far from Saturn

What is the origin of the different architecture?

Among Galilean satellites

Io & Europa: rocky satellite

Ganymede & Callisto: icy satellite

Callisto: undifferentiated

What is the origin of the satellites' diversity?

Overview of this study

Circum-Planetary Disk

Canup & Ward, 2002, 2006

Satellites formed in c.-p. disk

Actively-supplied accretion disk

Supplied from circum-stellar disk

→ Analytical solution for T , Σ

Satellite Formation

Ida & Lin, 2004, 2008, 2010

Analytical solution for

accretion timescale

type I migration timescale

trapping condition in MMR

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Adding New Ideas

Disk boundary conditions

Difference of Jovian/Saturnian systems is naturally reproduced?

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Canup & Ward (2002, 2006)

Actively-Supplied Accretion Disk

Uniform mass infall F_{in} from the circum-stellar disk

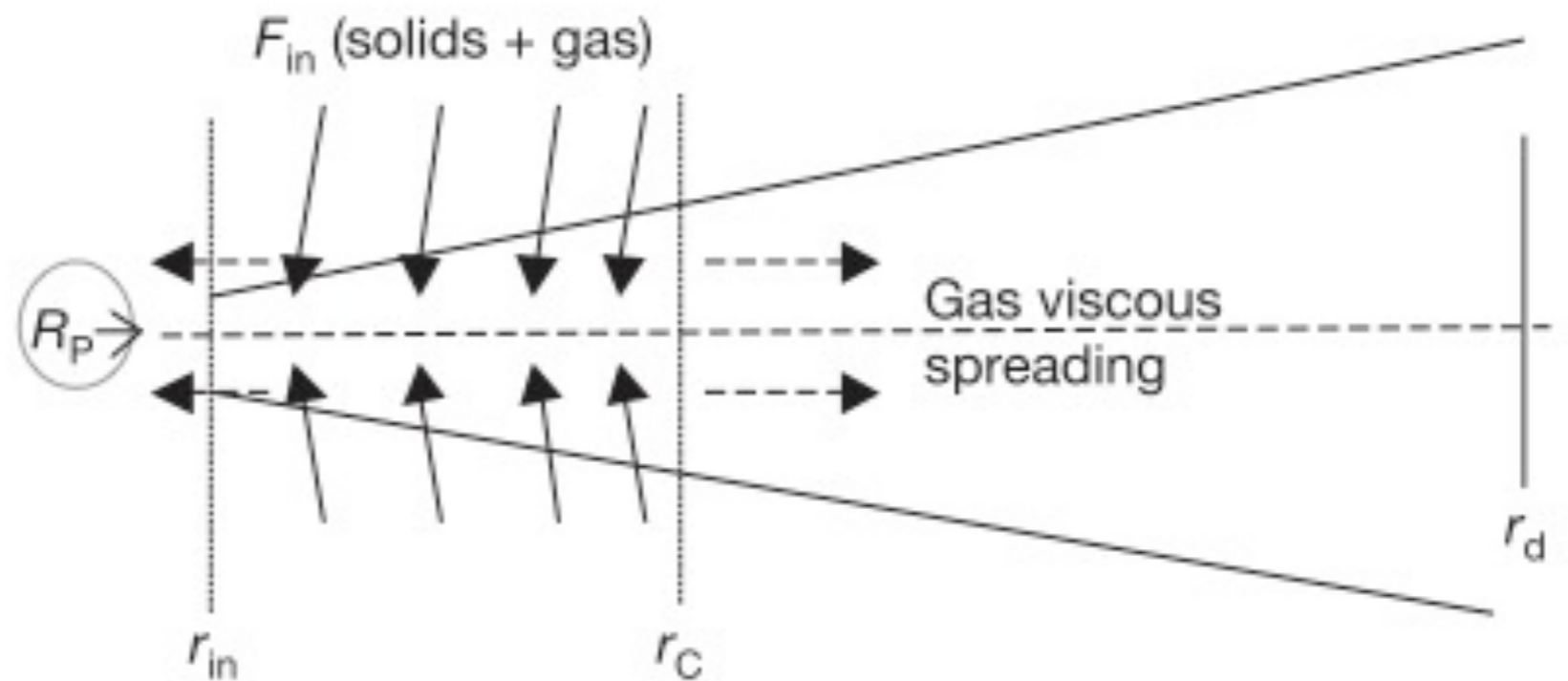
Infall regions: $r_{\text{in}} < r < r_{\text{c}}$ ($r_{\text{c}} \sim 30R_{\text{p}}$)

Diffuse out at outer edge: $r_{\text{d}} \sim 150R_{\text{p}}$

Infall rate decays exponentially with time

Temperature: balance of viscous heating and blackbody radiation

Viscosity: α model



Canup & Ward (2002, 2006) $+\alpha$

Inflow flux $F_{in} = F_{in}(t=0)\exp(-t/\tau_{in})$ [g/s]

Temperature $T_d \approx 160 \left(\frac{M_p}{M_J}\right)^{1/2} \left(\frac{\tau_G}{5 \times 10^6 \text{ yrs}}\right)^{-1/4} \left(\frac{r}{20R_J}\right)^{-3/4}$ [K]

Gas density $\Sigma_g \approx 100 f_g \left(\frac{M_p}{M_J}\right) \left(\frac{r}{20R_J}\right)^{-3/4}$ [g/cm²] $f_g \equiv \left(\frac{\alpha}{5 \times 10^{-3}}\right)^{-1} \left(\frac{\tau_G}{5 \times 10^6 \text{ yrs}}\right)^{-3/4}$

Dust density $\Sigma_d = \eta_{ice} f_d \left(\frac{M_p}{M_J}\right) \left(\frac{r}{20R_J}\right)^{-3/4}$ [g/cm²]

Increasing rate of dust density $\frac{df_d}{dt} = 0.029 \left(\frac{M_p}{M_J}\right)^{-2/3} \left(\frac{f}{100}\right)^{-1} \left(\frac{\tau_G}{5 \times 10^6 \text{ yrs}}\right)^{-1} \left(\frac{r}{20R_J}\right)^{3/4}$ [/years]

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Ida & Lin (2004, 2008, 2010)

Timescales of satellite's accretion & type I migration

$$\tau_{acc} = \frac{M}{\dot{M}} \approx 10^6 f_d^{-1} \eta_{ice}^{-1} \left(\frac{\rho}{\rho_p} \right)^{1/3} \left(\frac{M}{10^{-4} M_p} \right)^{1/3} \left(\frac{M_p}{M_J} \right)^{-5/6} \left(\frac{\beta}{10} \right)^2 \left(\frac{r}{20R_J} \right)^{5/4} \quad [\text{years}]$$

$$\tau_{mig} = \frac{r}{\dot{r}} \approx 10^5 \frac{1}{f_g} \left(\frac{M}{10^{-4} M_p} \right)^{-1} \left(\frac{M_p}{M_J} \right)^{-1} \left(\frac{r}{20R_J} \right)^{1/2} \left(\frac{\tau_G}{5 \times 10^6} \right)^{-1/4} \quad [\text{years}]$$

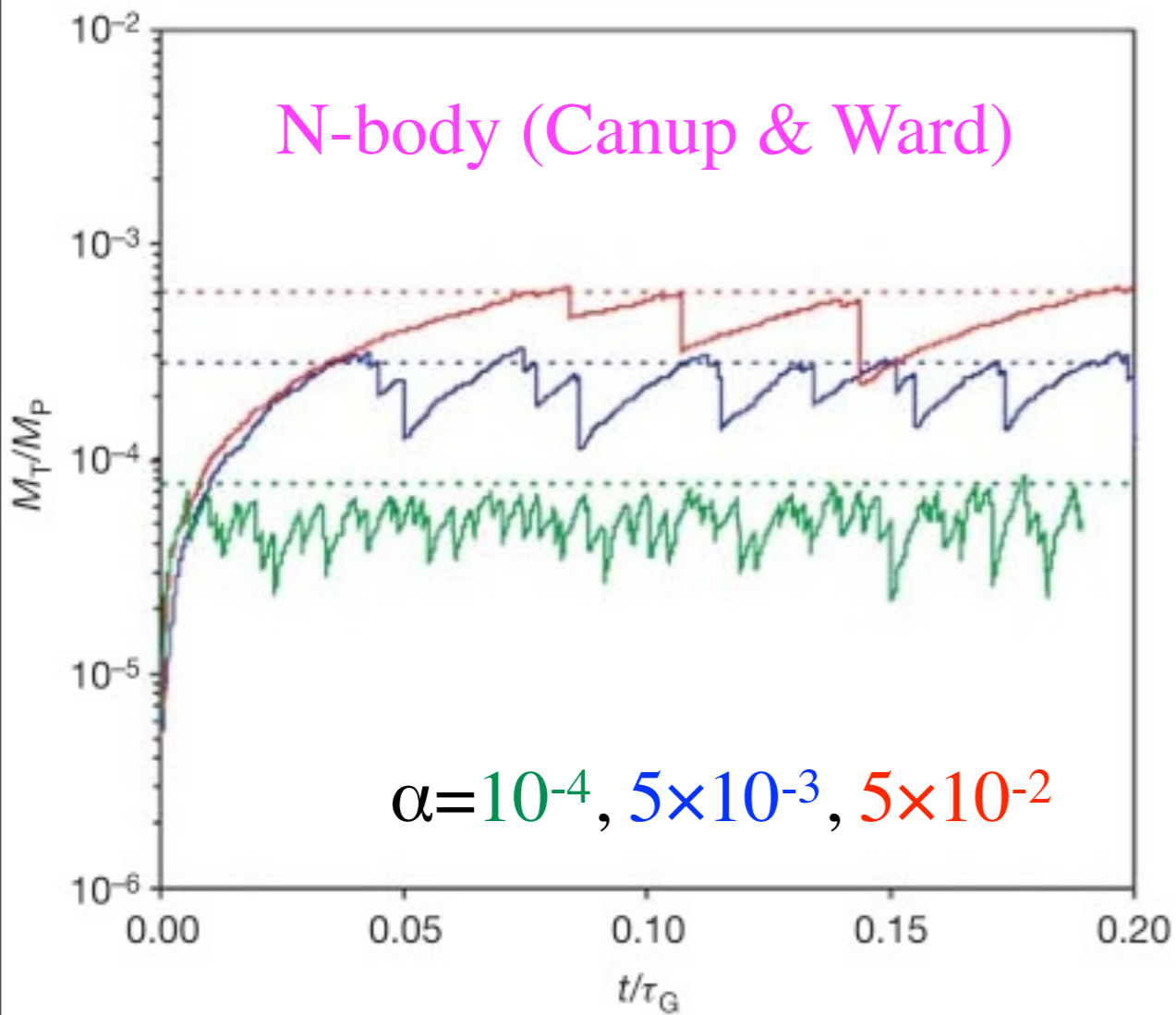
Resonant trapping width of migrating proto-satellites

$$b_{trap} = 0.16 \left(\frac{m_i + m_j}{M_{\oplus}} \right)^{1/6} \left(\frac{v_{mig}}{v_K} \right)^{-1/4} r_H \quad [\text{m}]$$

These approximate analytical solutions
are based on the results of N-body simulations

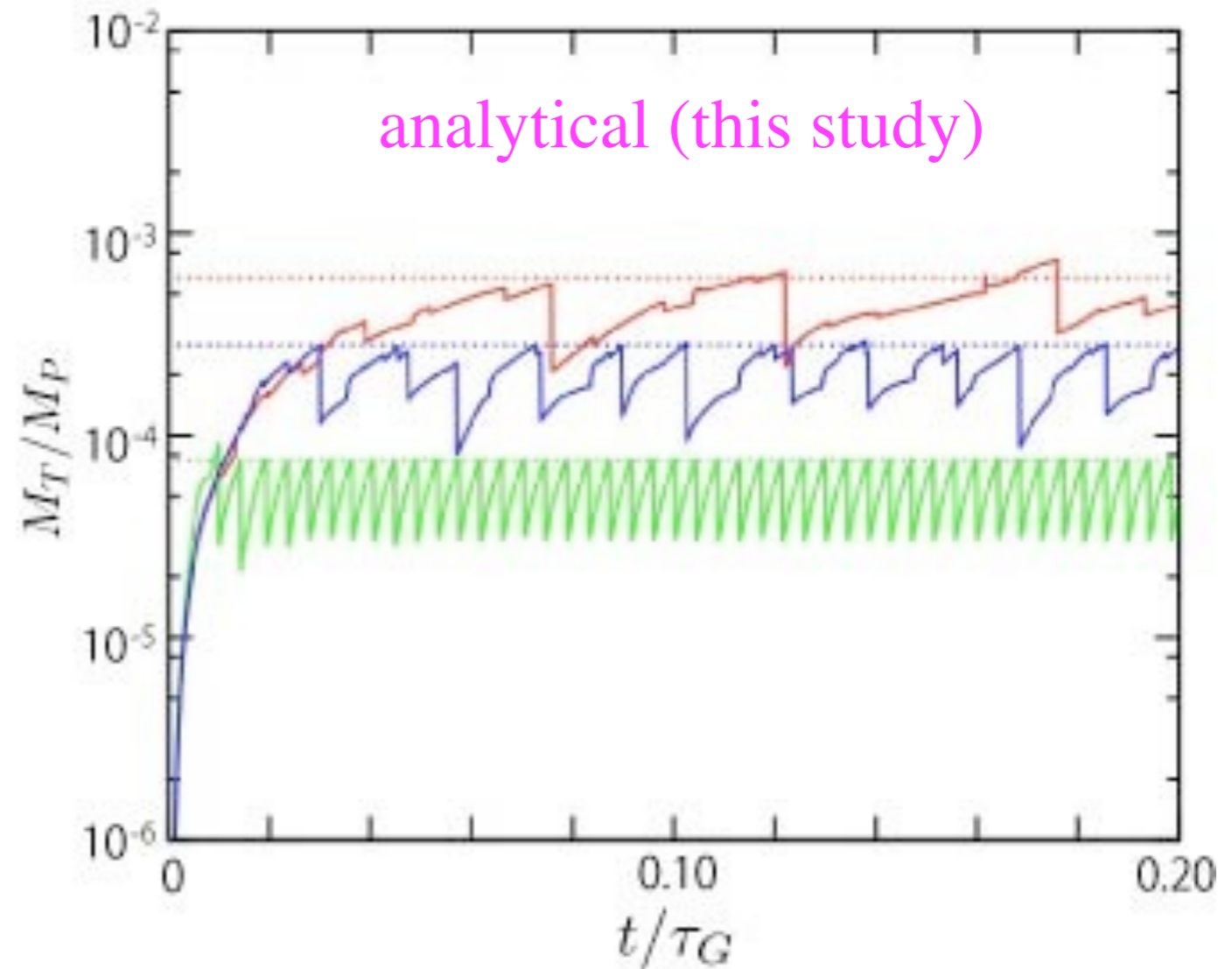
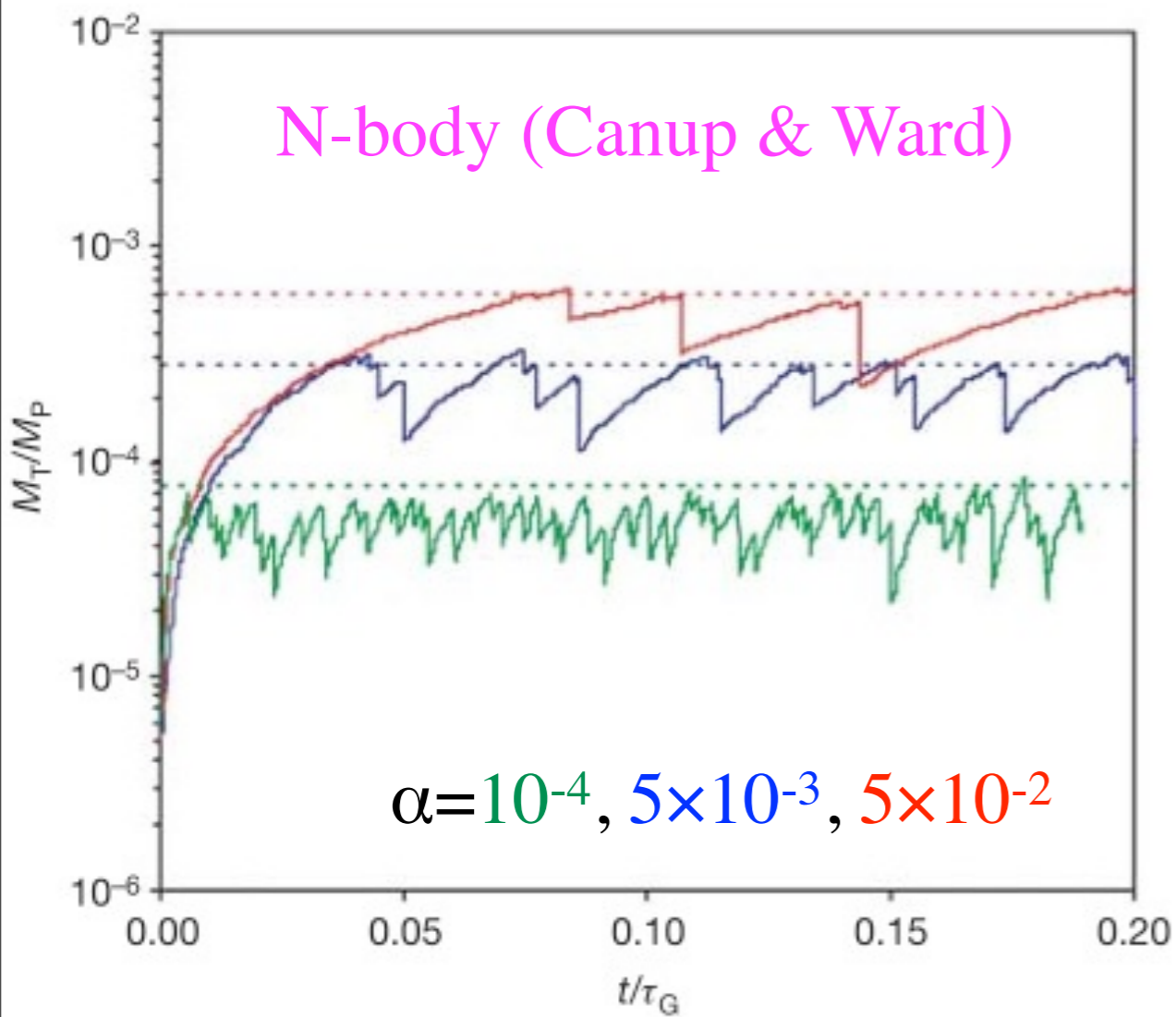
Comparison with N-body simulation

Time evolution of total mass of satellites (time-constant inflow)



Comparison with N-body simulation

Time evolution of total mass of satellites (time-constant inflow)



Excellent agreement with N-body simulation!

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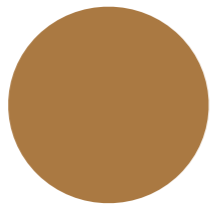
Adding New Ideas

Disk boundary conditions

Difference of Jovian/Saturnian systems is naturally reproduced?

The Ideas

Jupiter



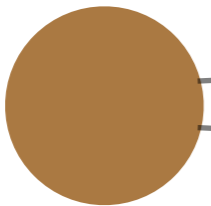
inner cavity



opened up gap in c.-s. disk

→ infall to c.-p. disk stop abruptly

Saturn



no cavity



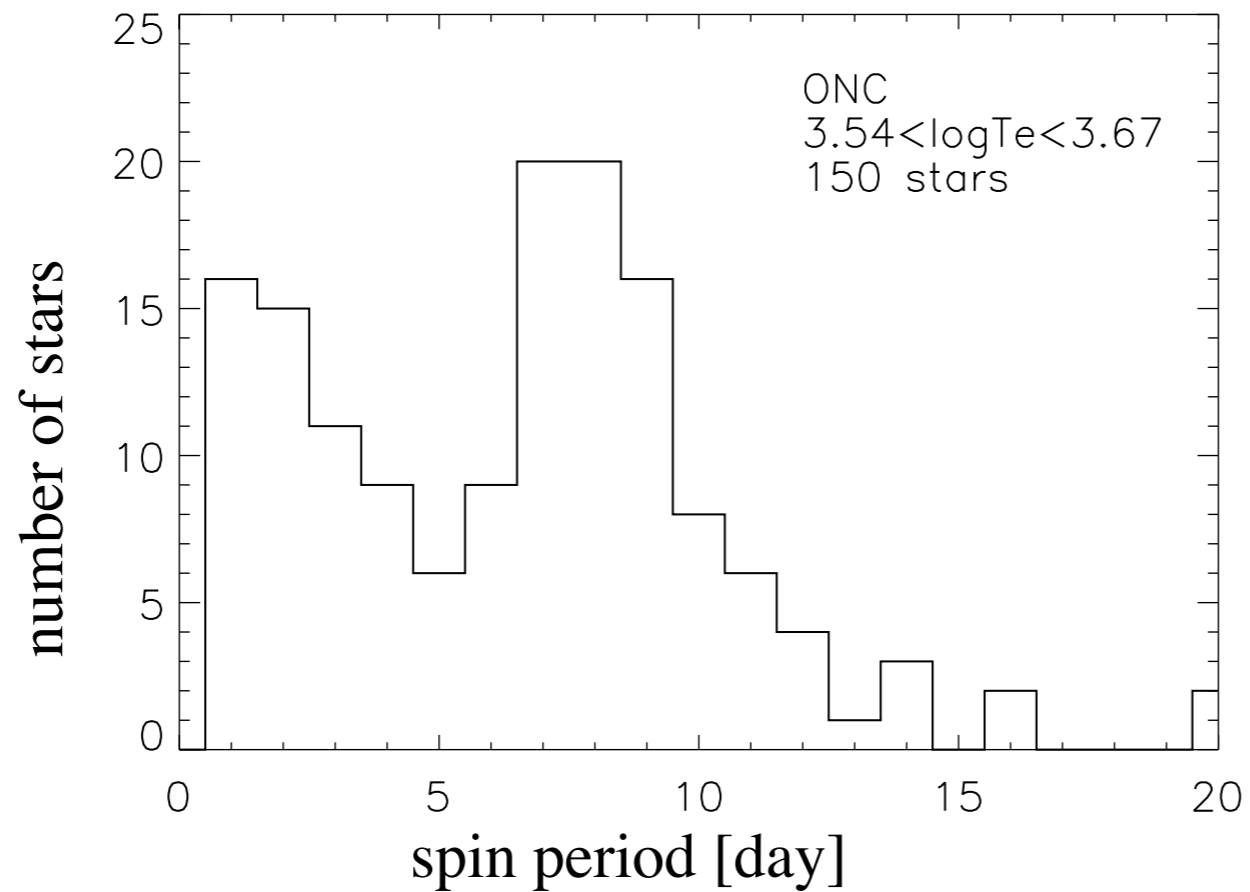
did not open up gap in c.-s. disk

→ c.-p. disk decay with c.-s. disk

Difference of “inner cavity” is from Königl (1991) and Stevenson (1974)

Difference of gap conditions is from Ida & Lin (2004)

Inner Cavity (Analogy with T-Tauri stars)

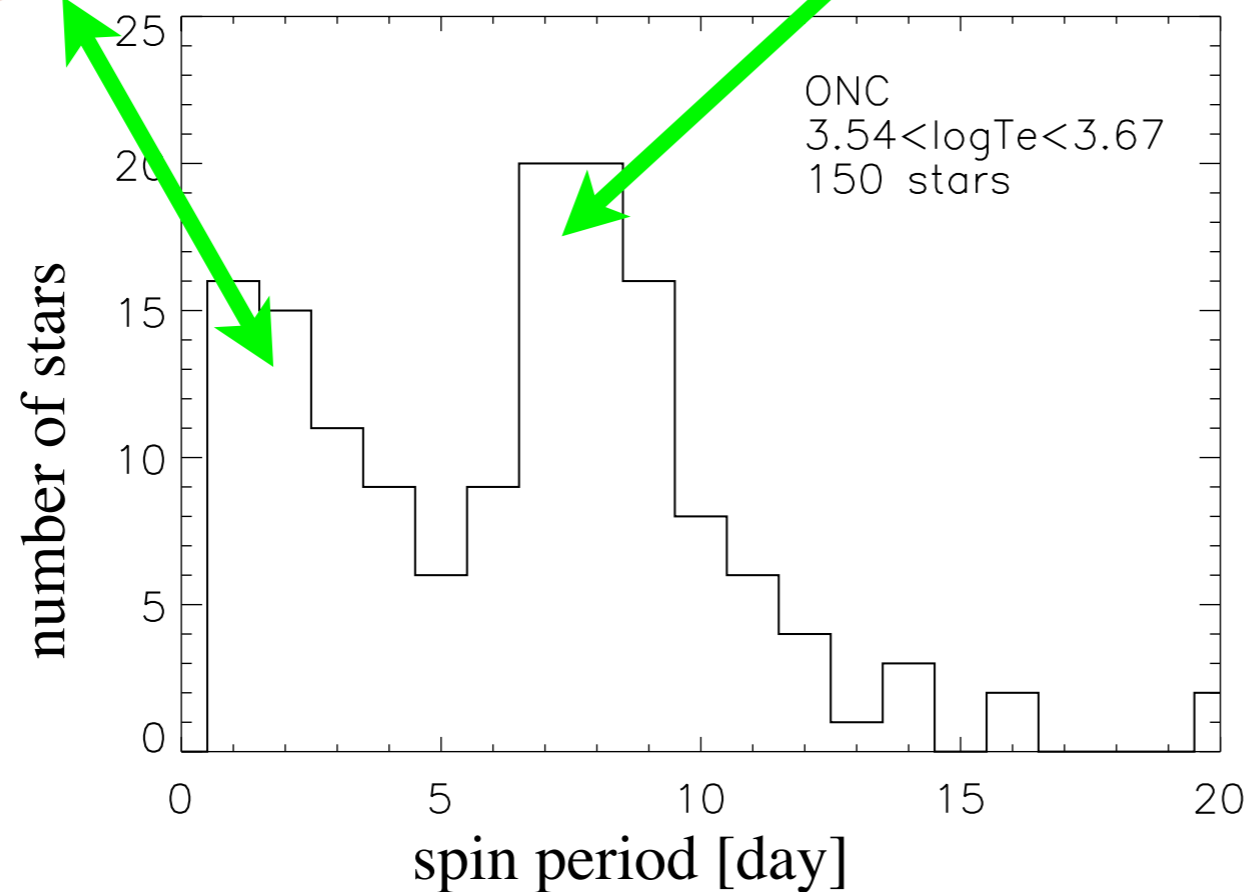
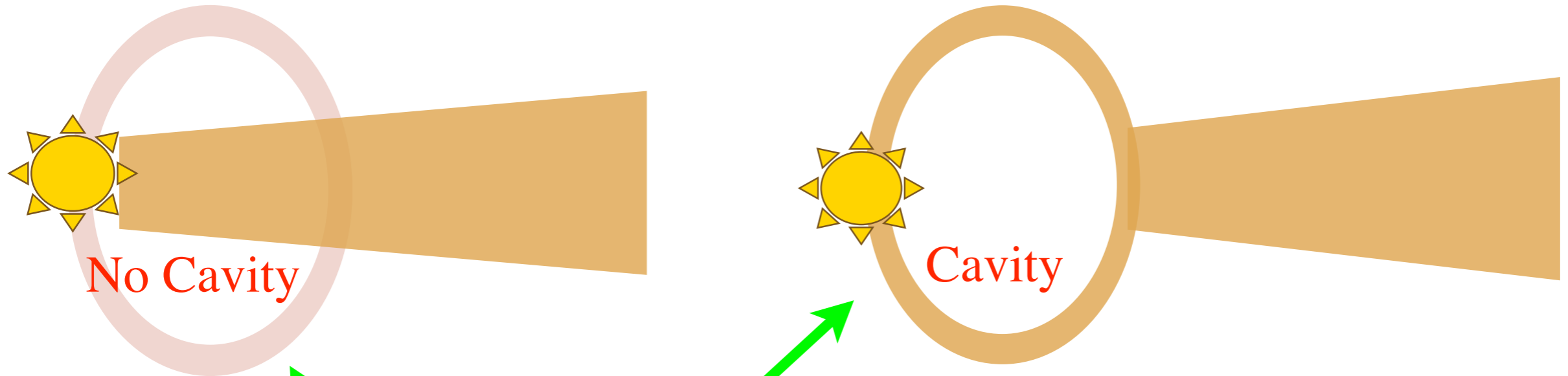


Herbst & Mundt (2005)

Inner Cavity (Analogy with T-Tauri stars)

weak magnetic field

strong magnetic field \rightarrow coupling with disk



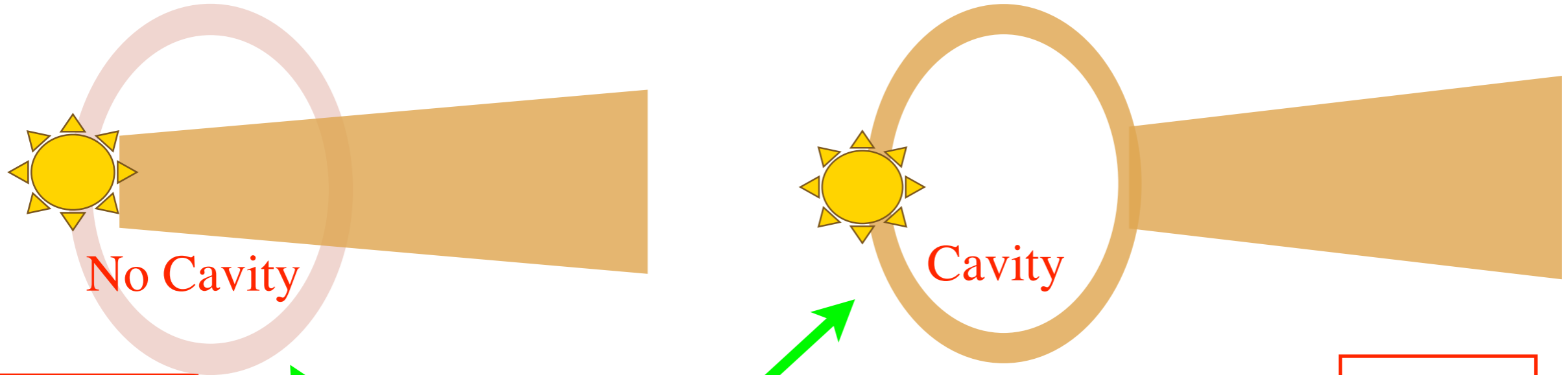
If the magnetic torque is stronger than the viscous torque, the disk would be truncated at the corotation radius

Herbst & Mundt (2005)

Inner Cavity (Analogy with T-Tauri stars)

weak magnetic field

strong magnetic field \rightarrow coupling with disk

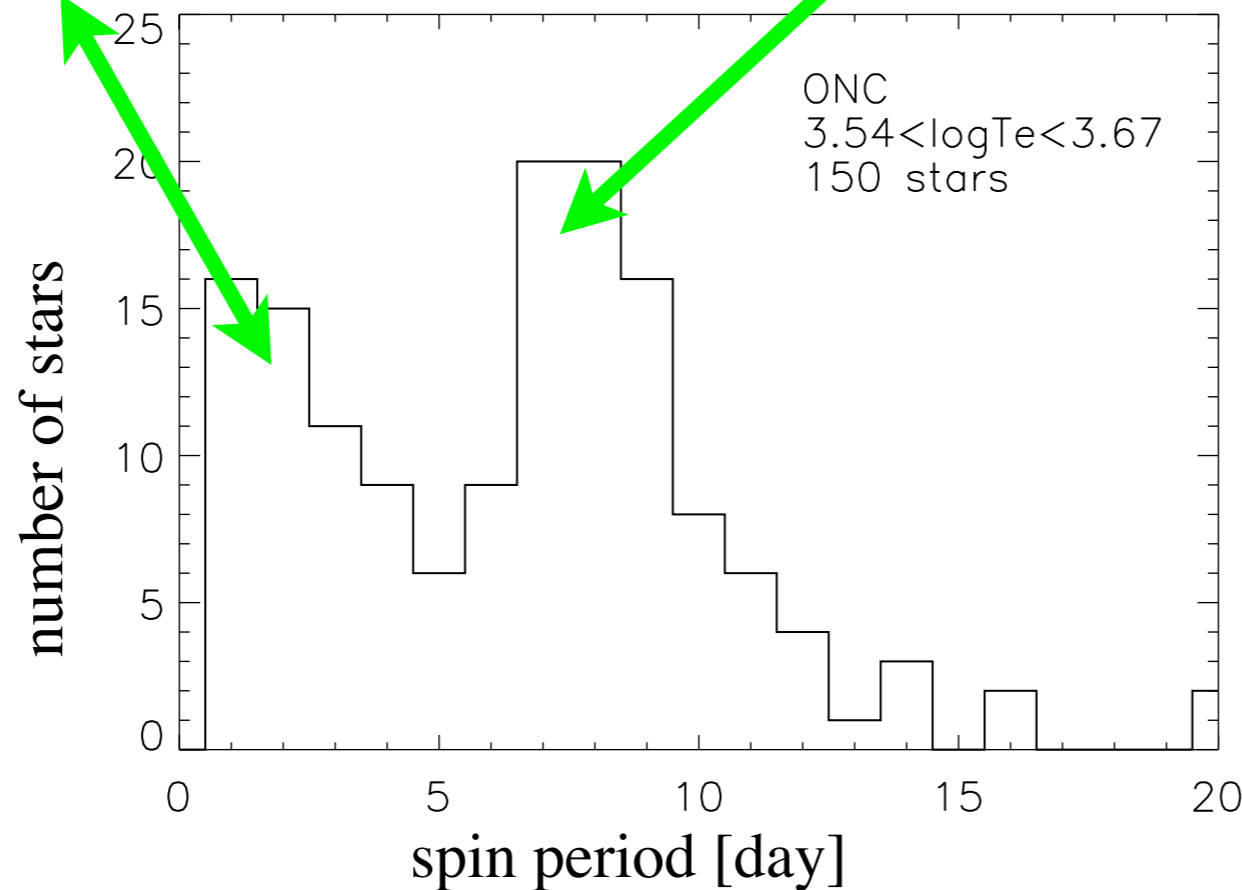


No Cavity

Cavity

Saturnian

Jovian



Herbst & Mundt (2005)

Estimates of Cavity Opening

Stevenson (1974)

proto-Jovian magnetic field ~ 1000 Gauss

Cavity

(Jovian system should be correspond to the stage)



Königl (1991)

magnetic field for the magnetic coupling

accretion rate $10^{-6}M_J/\text{yr} \rightarrow \sim$ a few hundred Gauss



Present Saturnian magnetic field < 1 Gauss

No Cavity

$\hat{=}$ late stage of Saturnian satellite formation

THE IDEAS

Jupiter: open up gap in circum-stellar disk

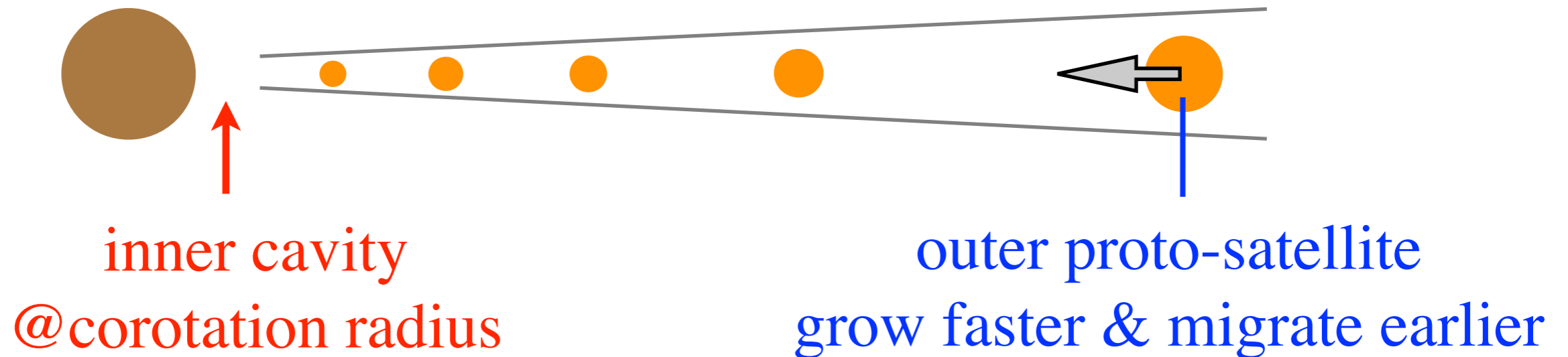
- infall to circum-planetary disk stop
- c.-p. disk quickly depleted
- frozen satellite system with “inner cavity”

Saturn: did not open up the gap

- c.-p. disk decay with c.-s. disk decay
- c.-p. disk slowly depleted
- satellite system without “inner cavity”

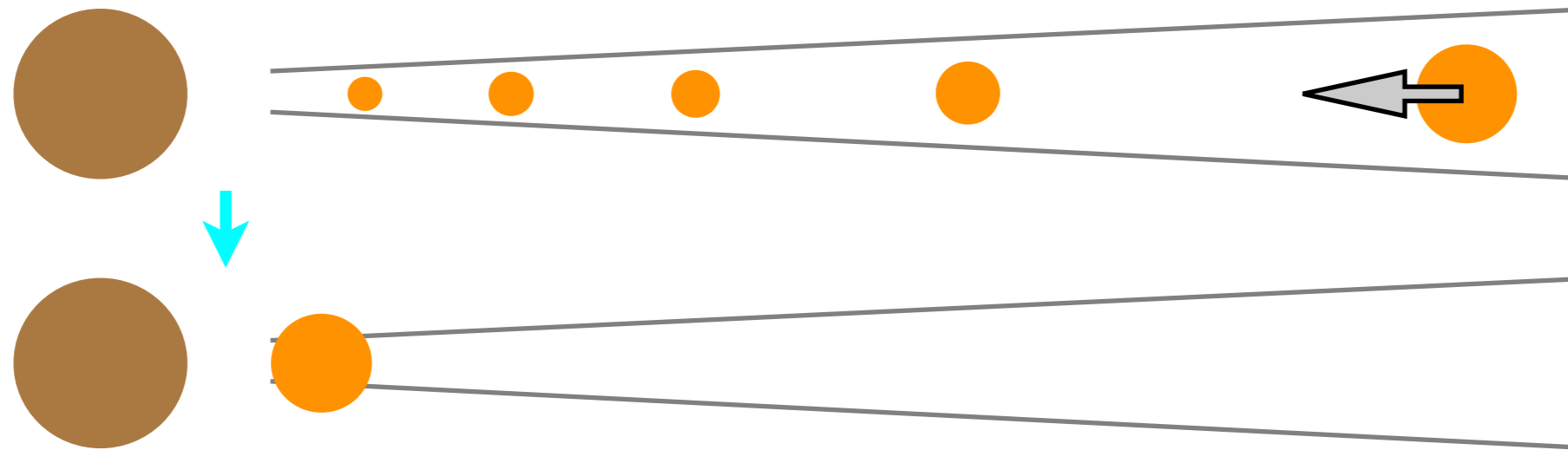
difference of gap conditions are from Ida & Lin (2004)

Jovian System



Because the infall mass flux per unit area is constant,
the total mass flux to satellite feeding zones is larger in outer regions.

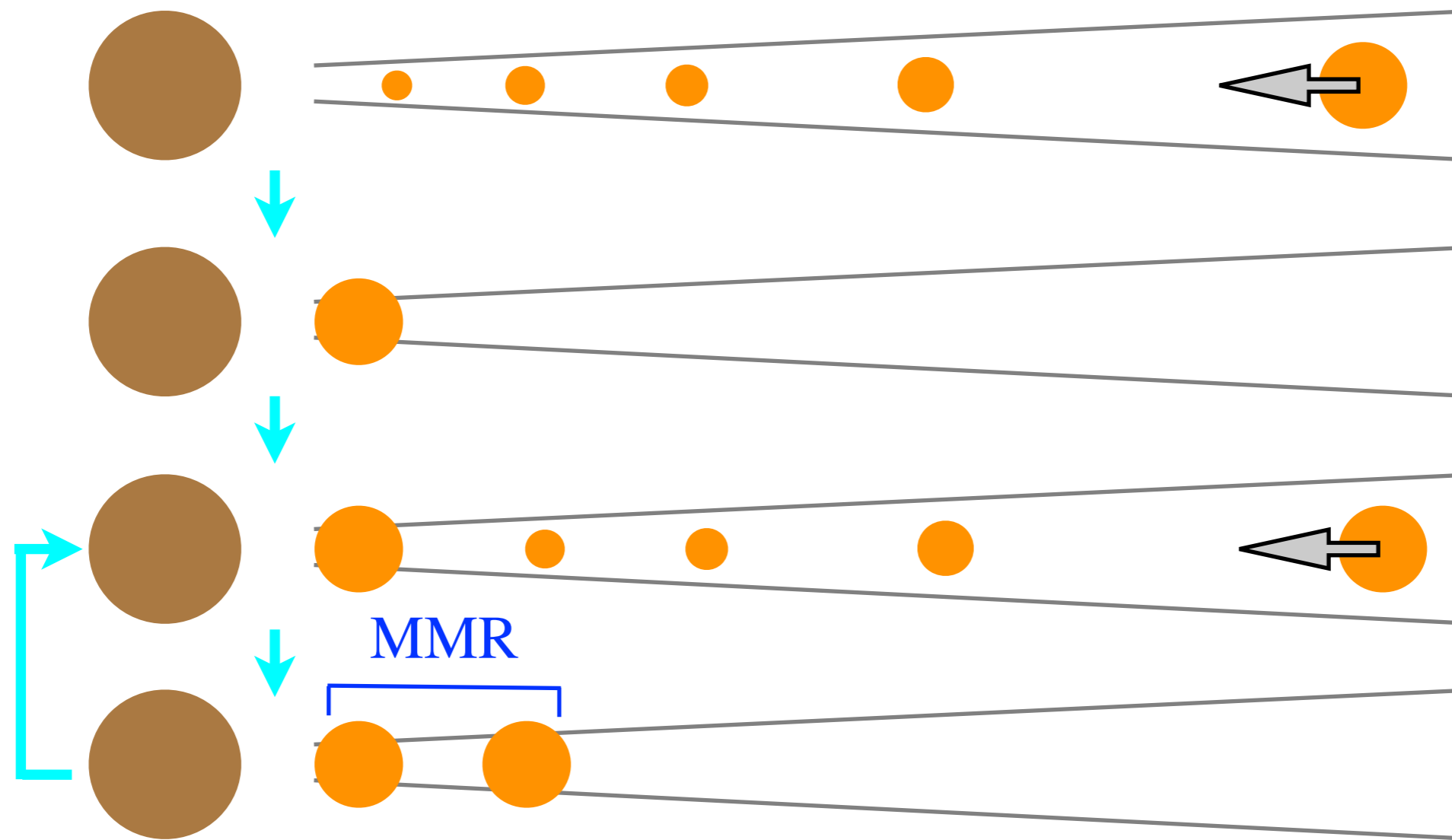
Jovian System



Type I migration is
halted near the inner edge

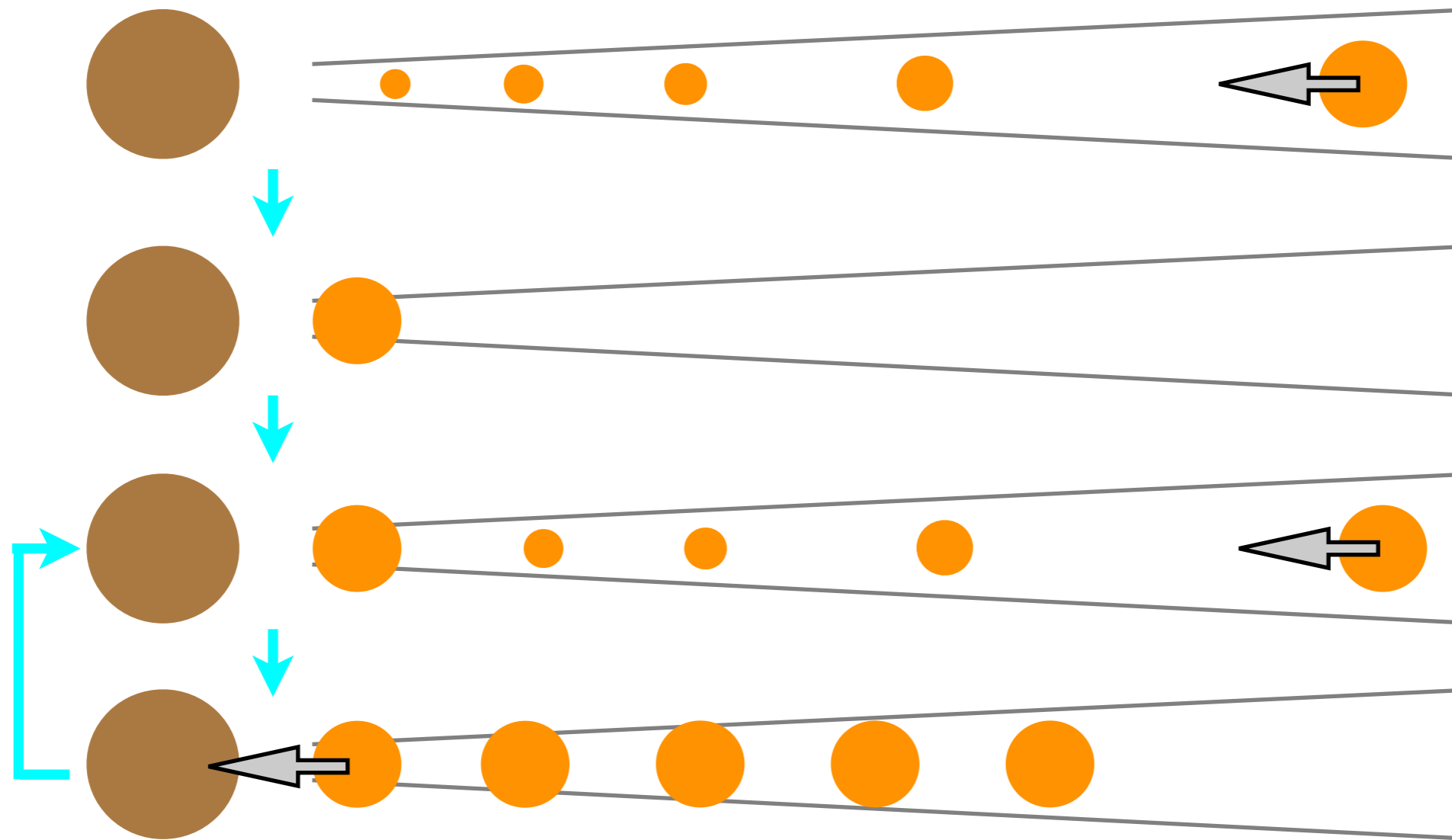
The outer most satellite migrates and sweeps up
the inner small satellites.

Jovian System



Proto-satellites grow & migrate repeatedly
They are trapped in MMR with the innermost satellite

Jovian System

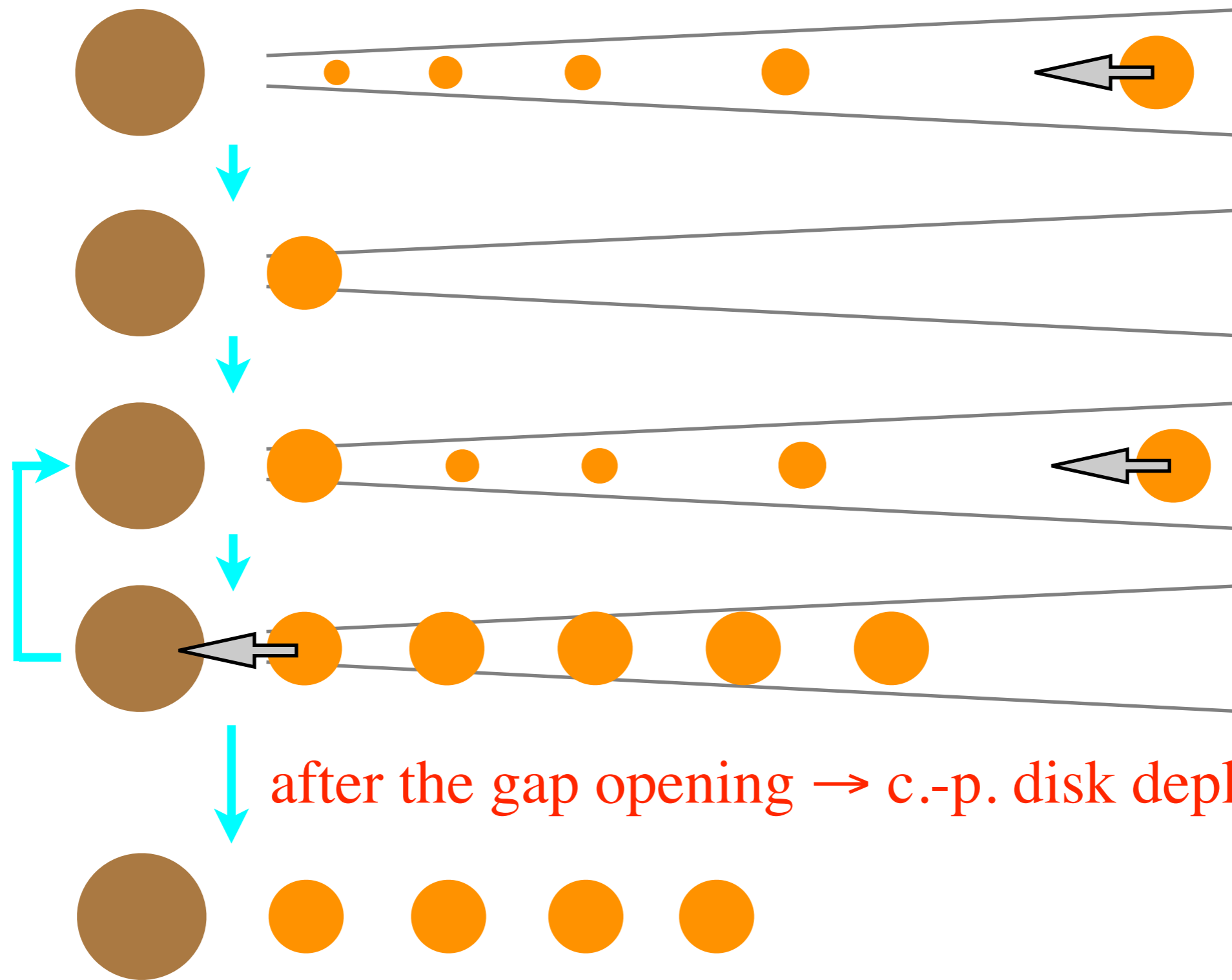


Total mass of the trapped satellites $>$ Disk mass

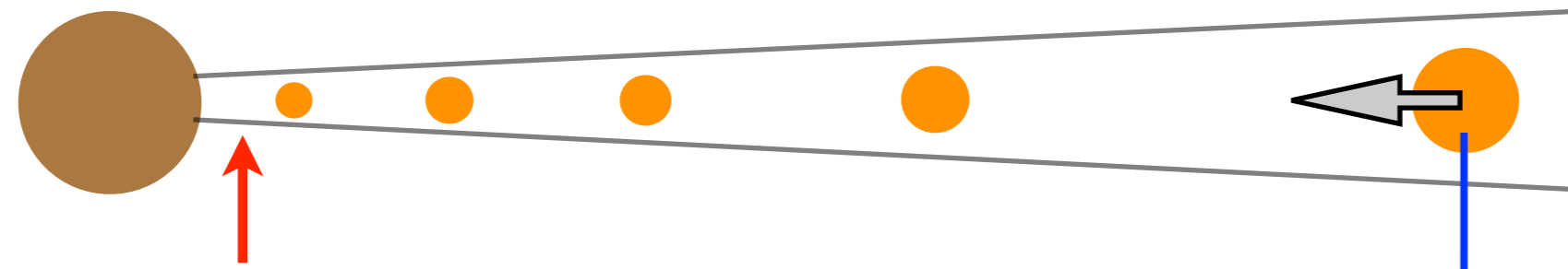
→ the halting mechanism is not effective

→ innermost satellite is released to the host planet

Jovian System



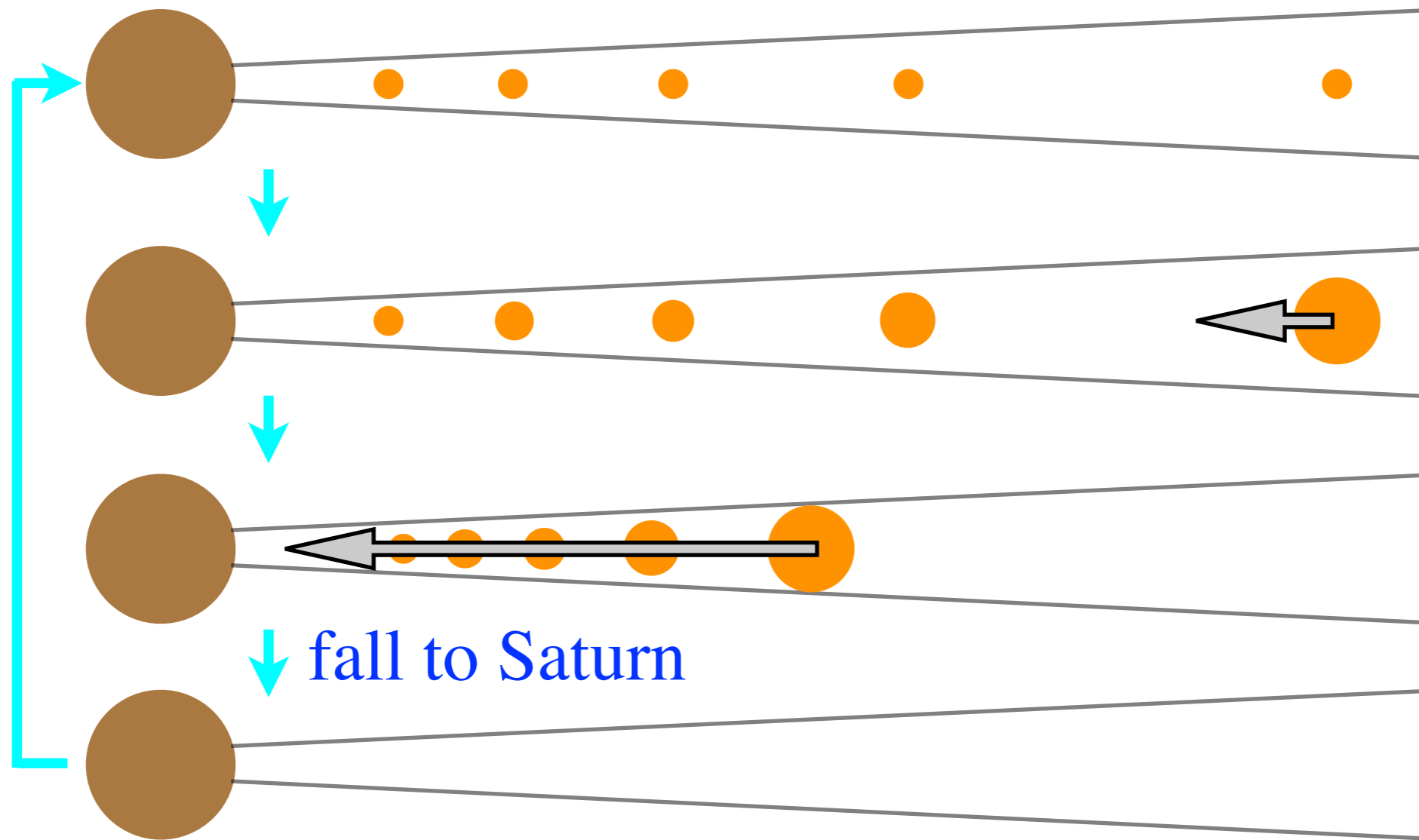
Saturnian System



No inner cavity

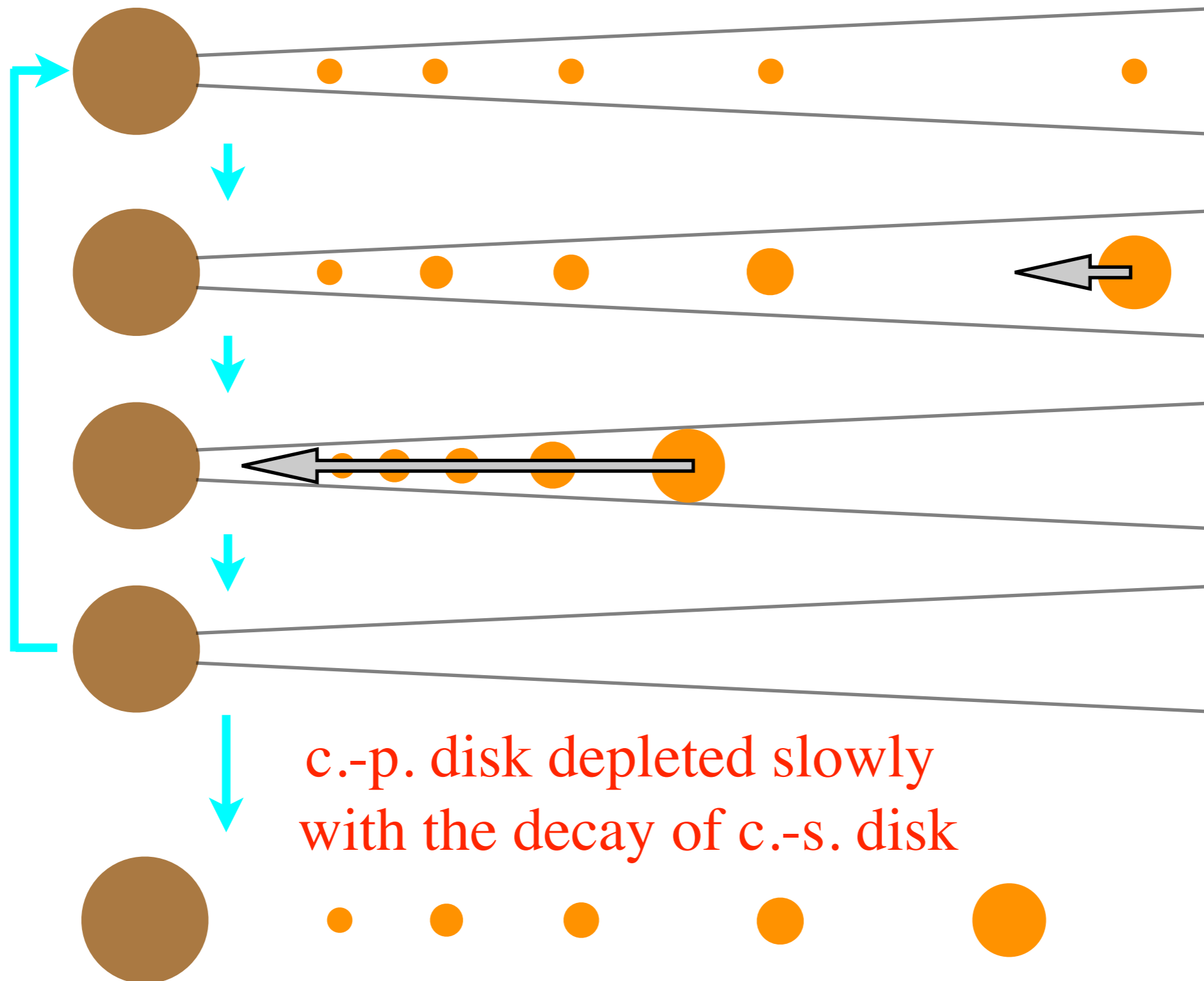
outer proto-satellite
grow faster & migrate earlier

Saturnian System



Large proto-satellites migrate from the outer regions and fall to the host planet with inner smaller satellites

Saturnian System



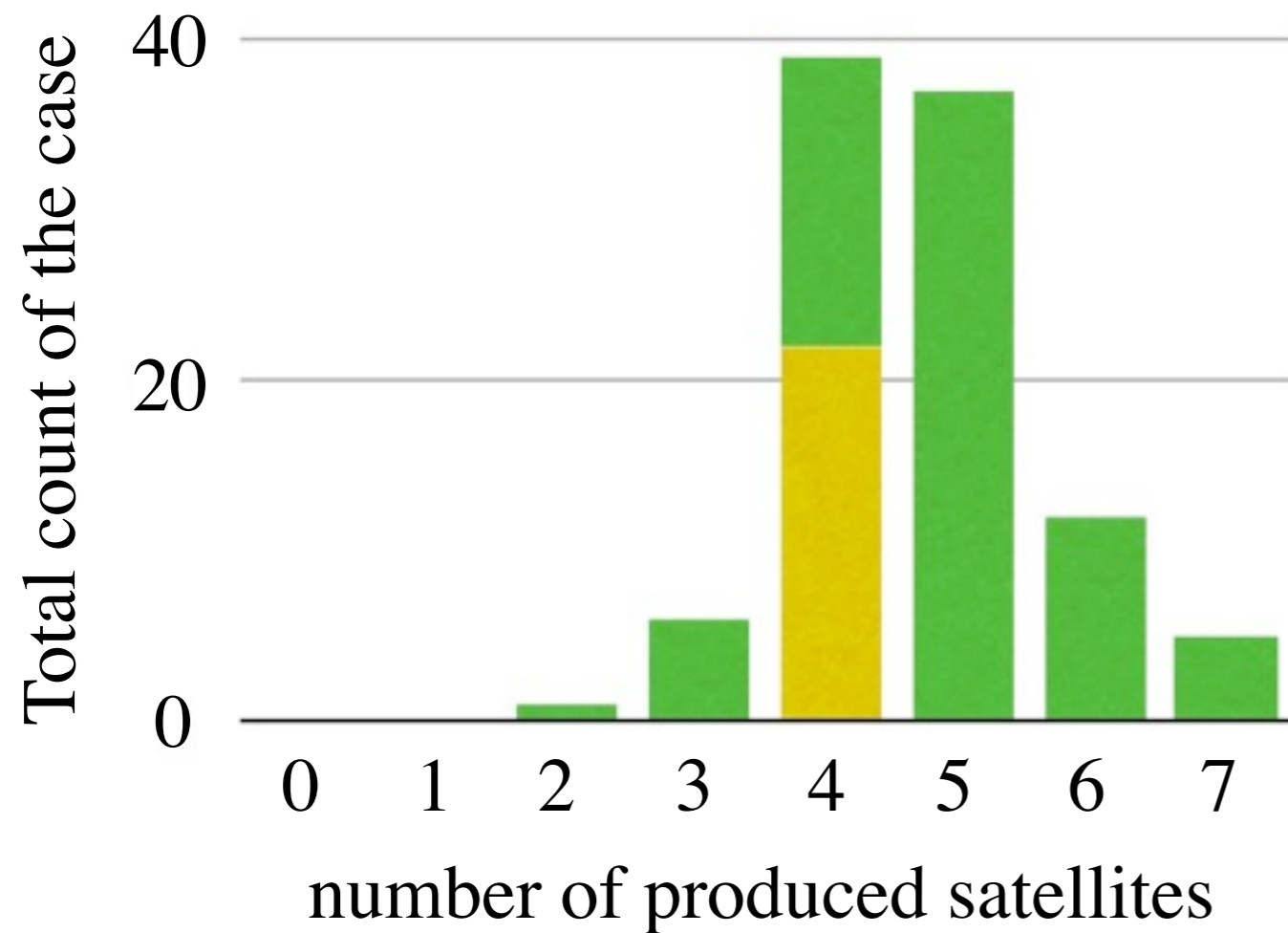
Monte Carlo Simulation (n=100)

Parameters:

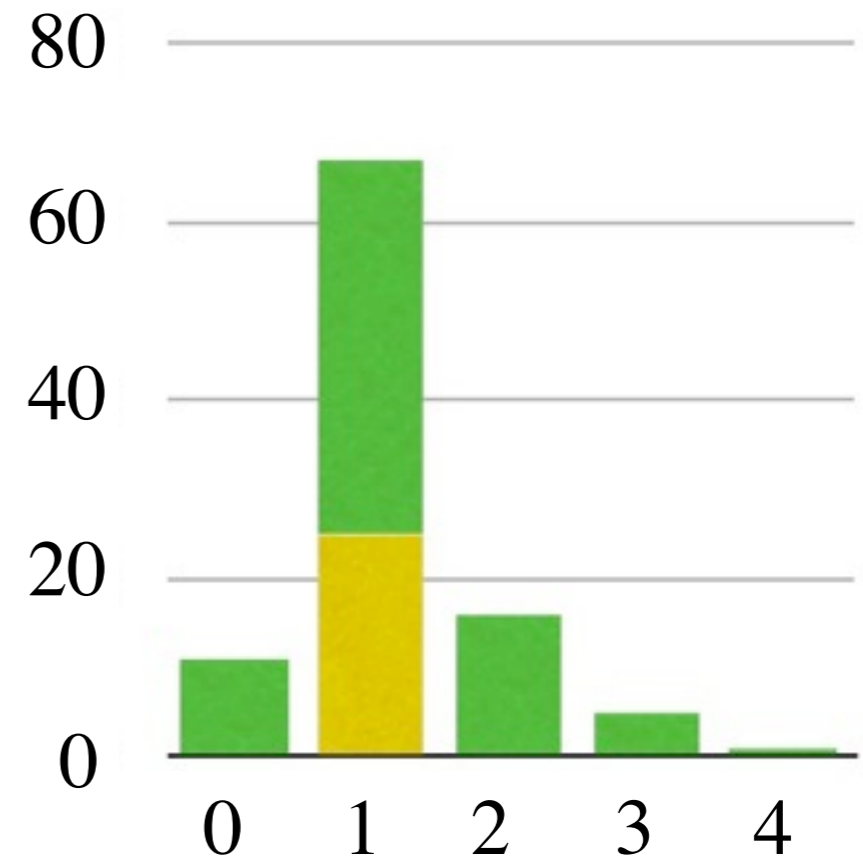
Disk viscosity (α model)	$\alpha = 10^{-3} - 10^{-2}$
Disk decay timescale	$\tau_{in} = 3 \times 10^6 - 5 \times 10^6 \text{ yr}$
Number of “satellite seeds”	$N = 10 - 20$

Results: Distribution of the number of large satellites

Jovian

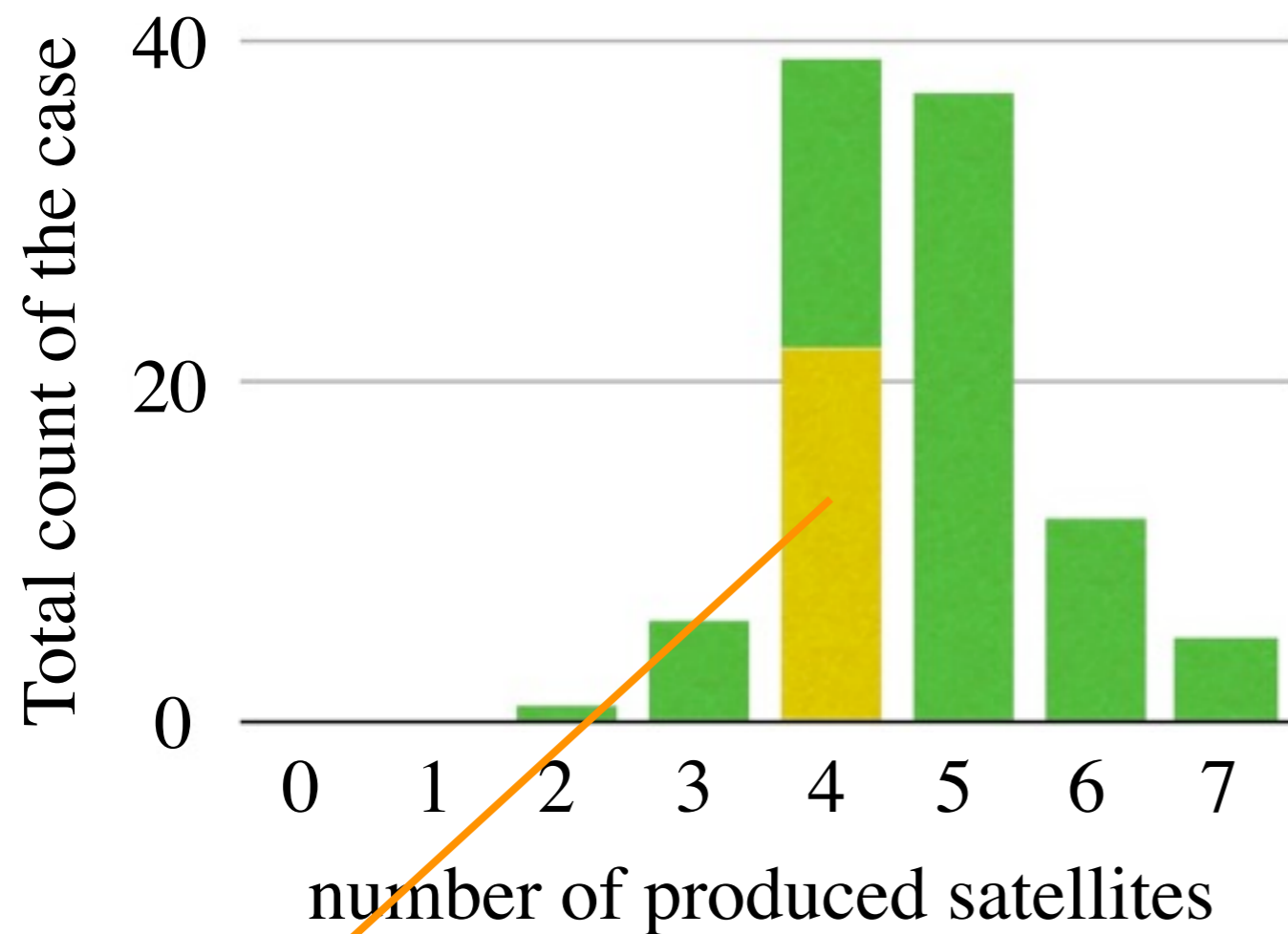


Saturnian

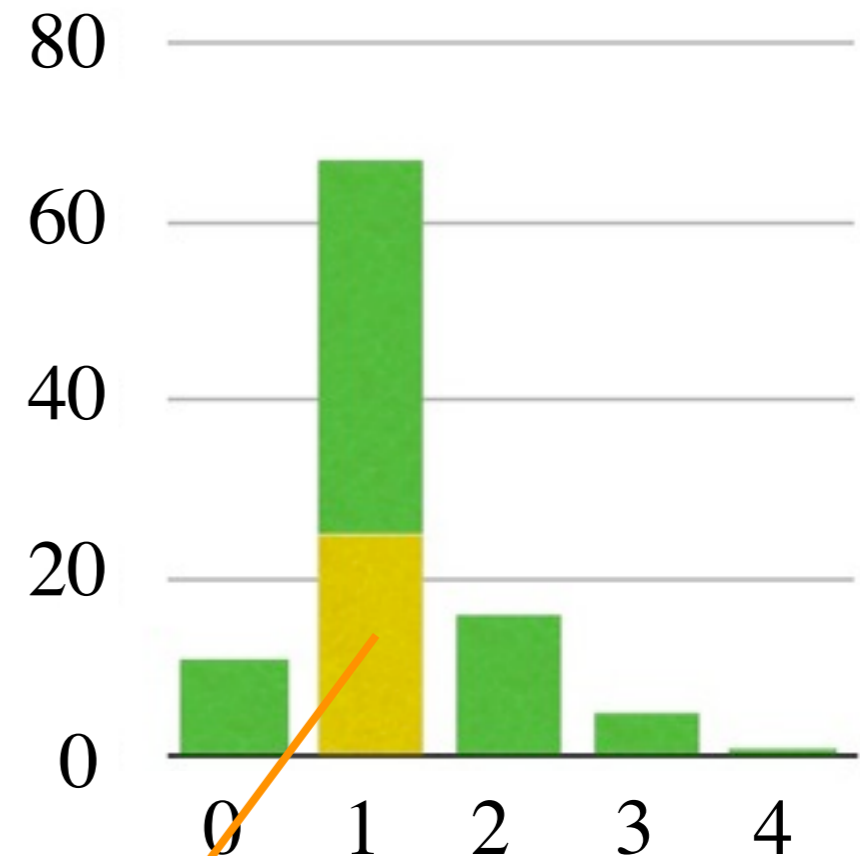


Results: Distribution of the number of large satellites

Jovian



Saturnian



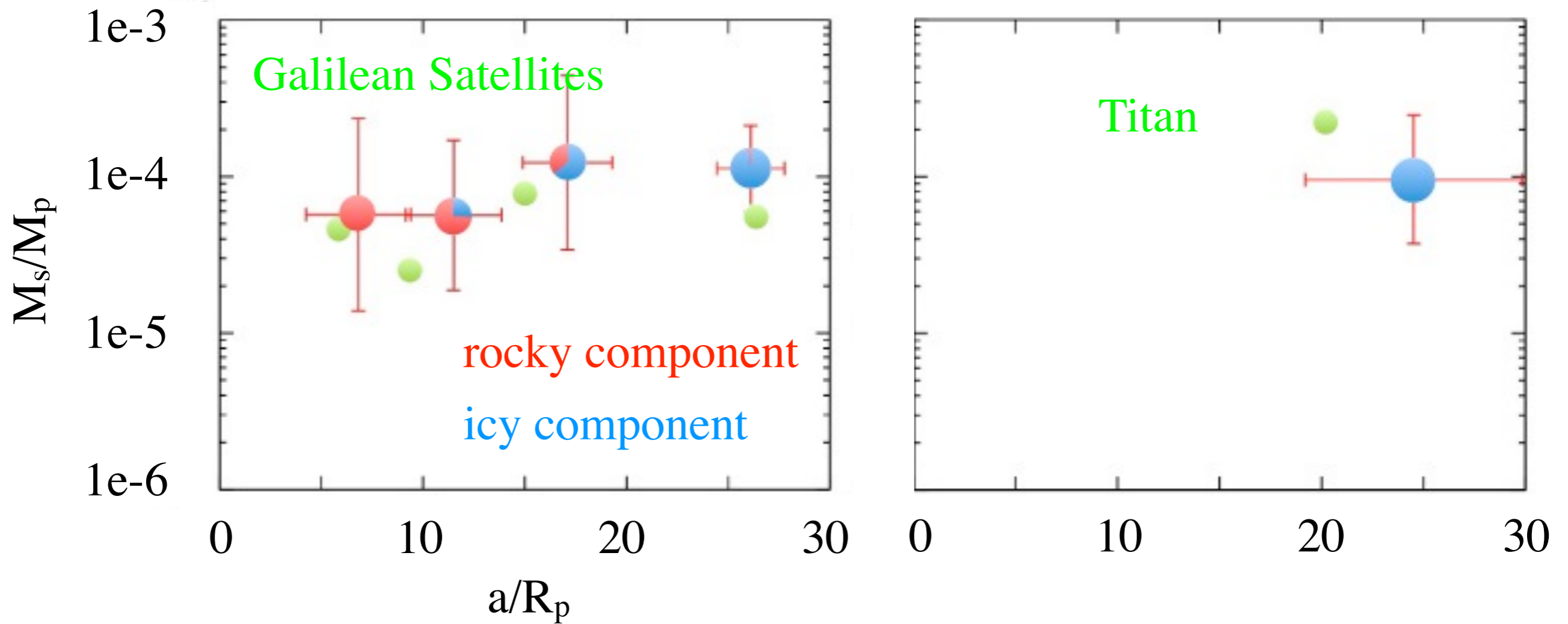
inner two bodies: rocky
& outer two bodies: icy

icy satellite
& large enough ($\sim M_{\text{Titan}}$)

Results: Properties of produced satellite systems

Jovian

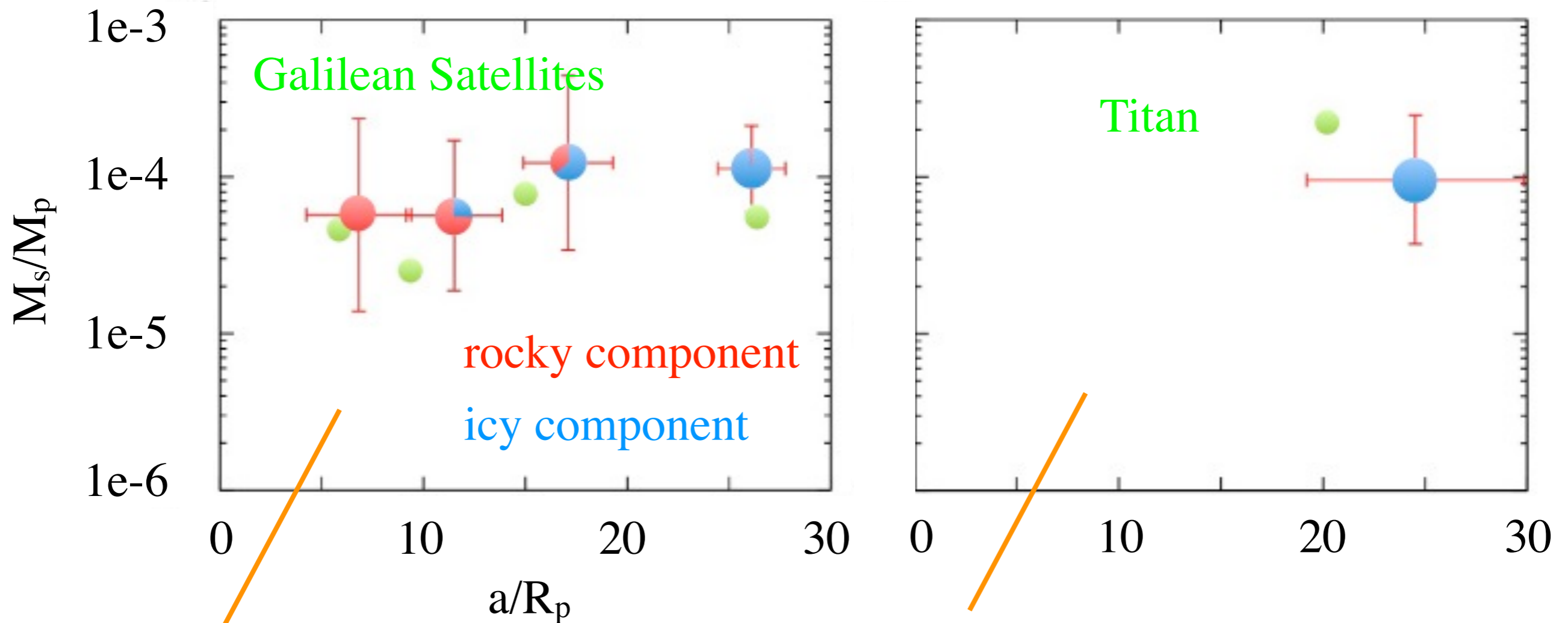
Saturnian



Results: Properties of produced satellite systems

Jovian

Saturnian



inner three bodies
are trapped in MMR

the largest satellite
has ~90% of total satellite mass

Results: Other features of produced satellite systems

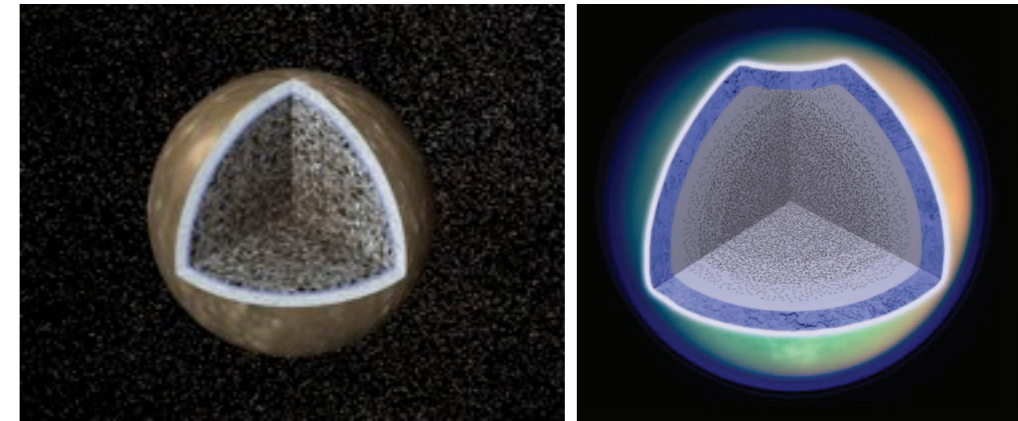
Callisto and Titan's undifferentiated interior

→ accretion timescales $> 5 \times 10^5$ years [Barr & Canup, 2008]

Accretion timescales in our simulations

Callisto: 10^5 - 10^6 years

Titan: $\sim 10^6$ years



Saturn's ring formed from an ancient satellite at Roche Zone

→ $R_{\text{Roche}} > R_{\text{Synch}}$ is required [Charnoz et al., 2009]

Jovian: $R_{\text{Roche}} < R_{\text{Synch}}$

Saturnian: $R_{\text{Roche}} > R_{\text{Synch}}$

Uranian, Neptunian: $R_{\text{Roche}} < R_{\text{Synch}}$



Summary

- **Jovian Satellite System v.s. Saturnian Satellite System**
Difference of size, number, location, and compositions
- **Satellite Accretion/Migration in Circum-Planetary Disk**
Canup & Ward (2002, 2006) + Ida & Lin (2004, 2008, 2010)
- **The Ideas of Disk Boundary Conditions**
Difference of inner cavity opening and gap opening conditions
- **Monte Carlo Simulations**
Difference of Jovian/Saturnian system are naturally reproduced

[Sasaki, Stewart & Ida (2010) *ApJ* **714**, 1052]